

Solving Linear Systems by Substitution

You can use substitution to solve a system of equations if one of the equations is already solved for a variable.

Example One: *When one equation is solved for a variable.*

(1) Choose one equation that is solved for x or y.

(2) Substitute the expression into the other equation and solve.

(3) Substitute the value found in step (2) to find the other variable.

$$5x + 2y = 9$$

$$y = (x + 8)$$

Solved for y

Substitute (x+8) in for y

$$5x + 2y = 9$$

$$5x + 2(x + 8) = 9$$

$$5x + 2x + 16 = 9$$

$$7x + 16 = 9$$

$$7x = -7$$

$$\frac{7x}{7} = \frac{-7}{7}$$

$$x = -1$$

Find y-value

$$y = x + 8$$

$$y = (-1) + 8$$

$$y = 7$$

* Can substitute in either equation.

Solution: $(-1, 7)$

Example Two: *When neither equation is solved for a variable.*

(1) Choose one equation and solve for x or y.

(2) Substitute the expression into the other equation and solve.

(3) Substitute the value found in step (2) to find the other variable.

$$2x + (y) = -1$$

$$-x + y = -7$$

$$y = (x - 7)$$

Substitute

$$2x + y = -1$$

$$2x + (x - 7) = -1$$

$$3x - 7 = -1$$

$$+7 \quad +7$$

$$3x = 6$$

$$\frac{3x}{3} = \frac{6}{3}$$

$$x = 2$$

Find y-value

$$y = x - 7$$

$$y = (2) - 7$$

$$y = -5$$

Solution: $(2, -5)$